

Trigonometric Equations

Question1

If $\cos x + \cos^2 x = 1$, then the value of $\sin^2 x + \sin^4 x$ is

KCET 2025

Options:

- A. -1
- B. 1
- C. 0
- D. 2

Answer: B

Solution:

$$\begin{aligned}\cos x + \cos^2 x &= 1 \\ \Rightarrow 1 - \cos^2 x &= \cos x \quad \Rightarrow \sin^2 x = \cos x \\ \Rightarrow \sin^2 x + \sin^4 x & \\ \Rightarrow \cos x + (\cos x)^2 &= 1\end{aligned}$$

Question2

The trigonometric function $y = \tan x$ in the II quadrant

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Options:



- A. decreases from 0 to ∞
- B. decreases from $-\infty$ to 0
- C. increases from 0 to ∞
- D. increases from $-\infty$ to 0

Answer: D

Solution:

Given, function $y = \tan x$

We know that, $\tan x$ is increasing in all the quadrants and for II quadrant the value of x is considered as $(-\infty, 0)$.

Hence, $y = \tan x$ increase from $-\infty$ to 0.

Question3

If $\cos x = |\sin x|$ then, the general solution is

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Options:

- A. $x = n\pi + (-1)^n \frac{\pi}{4}, n \in Z$
- B. $x = n\pi \pm \frac{\pi}{4}, n \in Z$
- C. $x = (2n + 1)\pi \pm \frac{\pi}{4}, n \in Z$
- D. $x = 2n\pi \pm \frac{\pi}{4}, n \in Z$

Answer: D

Solution:



We have, $|\sin x| = \cos x$

$$\Rightarrow \sin^2 x = \cos^2 x \Rightarrow 2 \cos^2 x = 1$$

$$\Rightarrow \cos x = \frac{1}{\sqrt{2}} \text{ (since, } \cos x \text{ can not be negative)}$$

$$\Rightarrow x = 2n\pi \pm \frac{\pi}{4}$$

